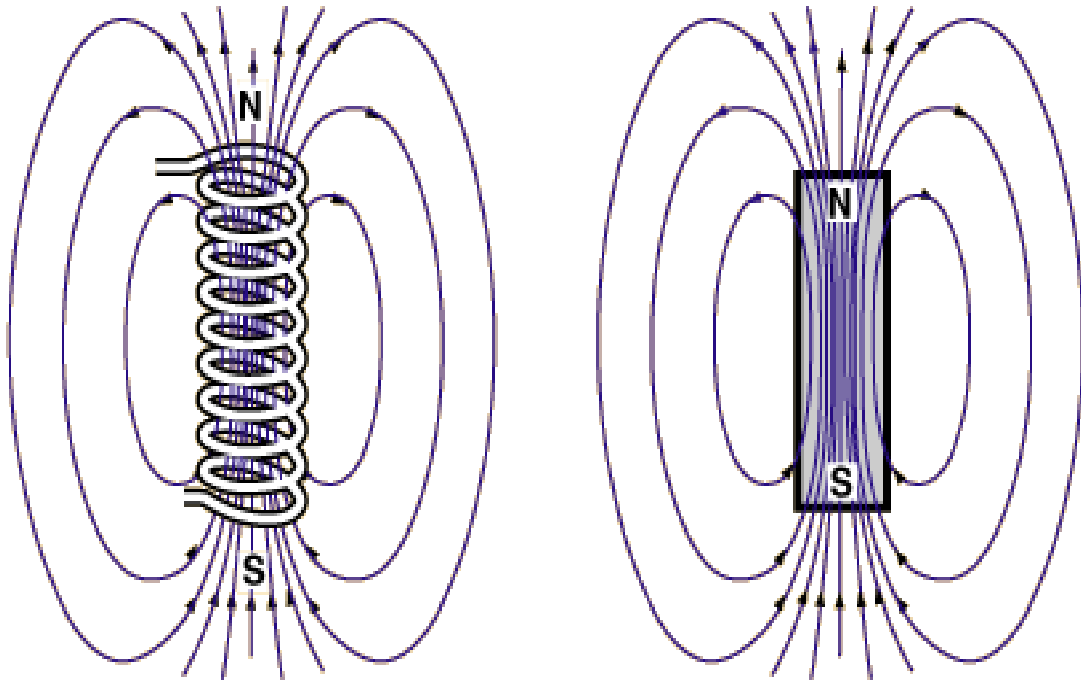
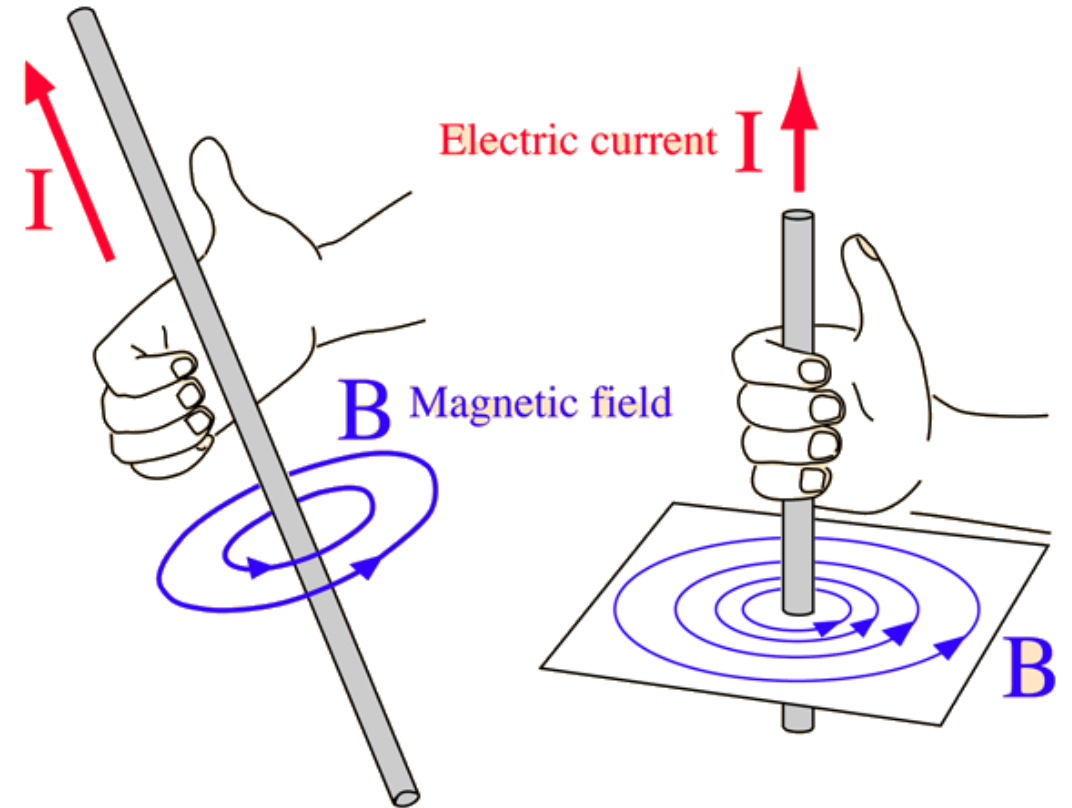


# Magnetic field created by current

## 1. Permanent Magnet



## 2. Current



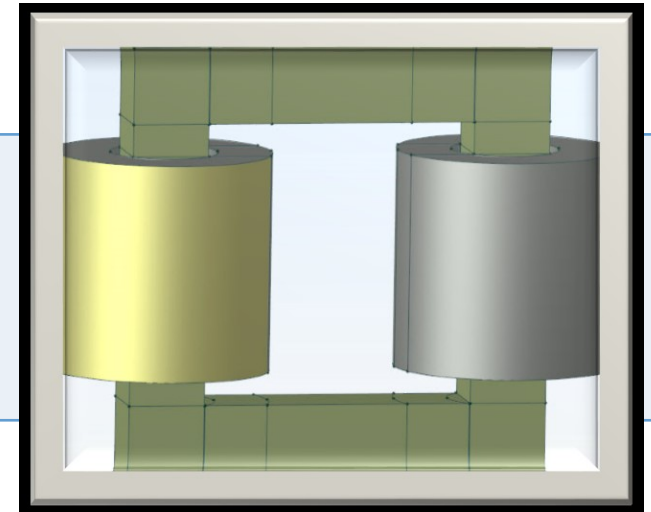
# Magnetic field created by current

- 1 How to set current in QuickField:
- Volume current density / total current
  - Surface current density (by Neumann boundary condition)
  - Linear current

- 2 Magnetostatic is about DC currents.  
What to do with AC devices?

- 3 Let's practice with the transformer:
1. Idle-run test
  2. Short-circuit test

- 5 How to extract results:  
Flux linkage, Inductance, Induced EMF



# Magnetic field created by current

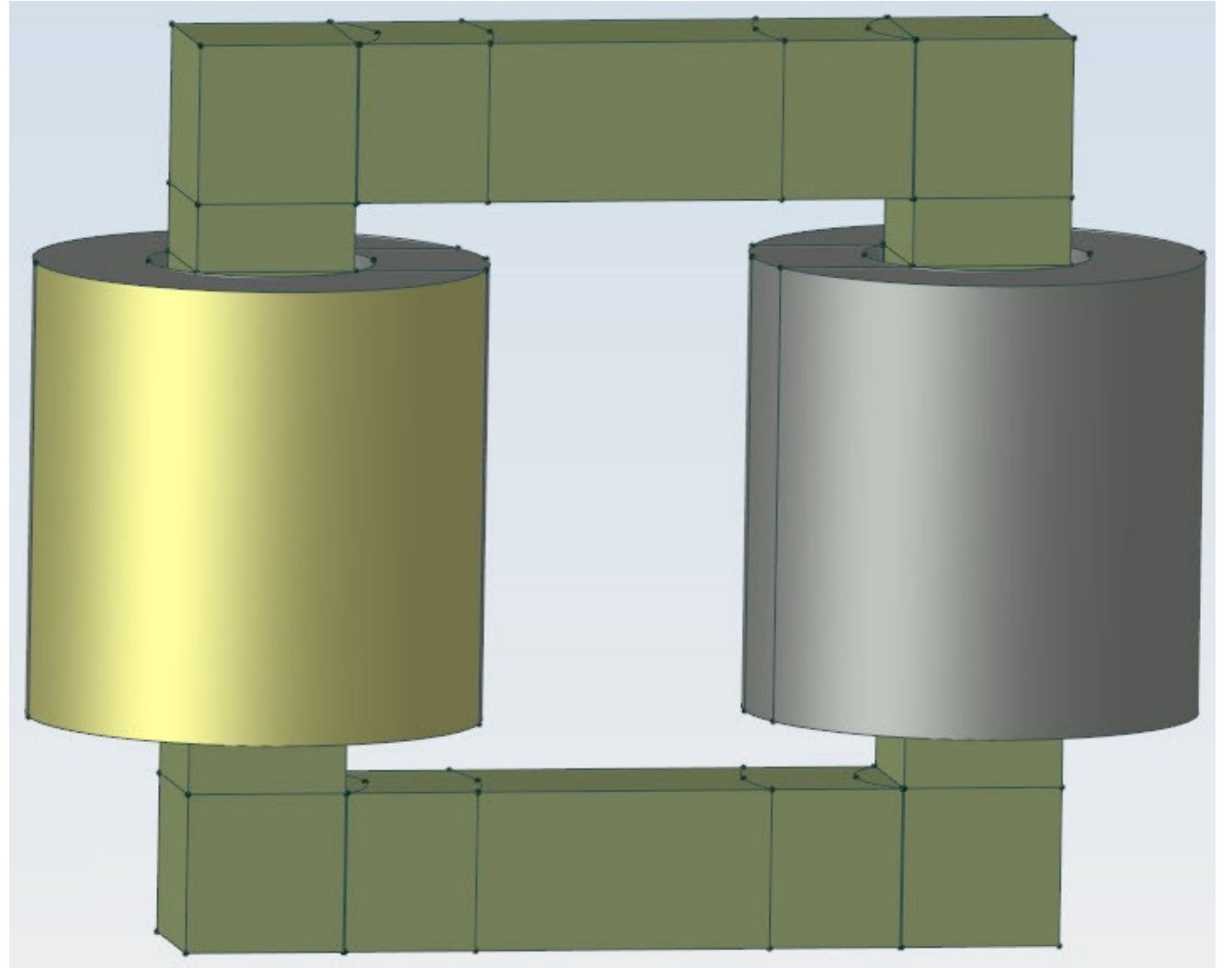
| What            | Where                                                                                                                                                                                                                                                 | How                                                                                                                                                                                                                                                                                                                                                                                                                  |
|-----------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Volume current  | Block <ul style="list-style-type: none"> <li>Given current density (<math>\text{A/m}^2</math>)</li> <li>Total Ampere-turns (A)               <ul style="list-style-type: none"> <li>Parallel / Serial (for total current only)</li> </ul> </li> </ul> | <div>Field Source</div> <div> <math>I = </math> <input type="text" value="0.12 * 380"/> (A)           </div> <div> <input type="radio"/> Current Density           <input checked="" type="radio"/> Total Ampere-Turns         </div> <div> <div>Conductor's Connection</div> <div> <input checked="" type="radio"/> In Parallel           <input type="radio"/> In Series         </div> </div> <div><b>f</b></div> |
| Surface current | Edge <ul style="list-style-type: none"> <li>Surface current density (<math>\text{A/m}</math>) (can depend on coordinates)</li> </ul>                                                                                                                  | <div> <input checked="" type="checkbox"/> Tangential Field: <math>H_t = \sigma</math> (<math>\Delta H_t = \sigma</math>)         </div> <div> <math>\sigma = </math> <input type="text" value="100"/> (<math>\text{A/m}</math>)         </div>                                                                                                                                                                       |
| Linear current  | Vertex <ul style="list-style-type: none"> <li>Given current (A)</li> </ul>                                                                                                                                                                            | <div> <input checked="" type="checkbox"/> Linear Current         </div> <div> <math>I = </math> <input type="text" value="155"/> (A)         </div>                                                                                                                                                                                                                                                                  |

# The simple transformer

## 1. Photo

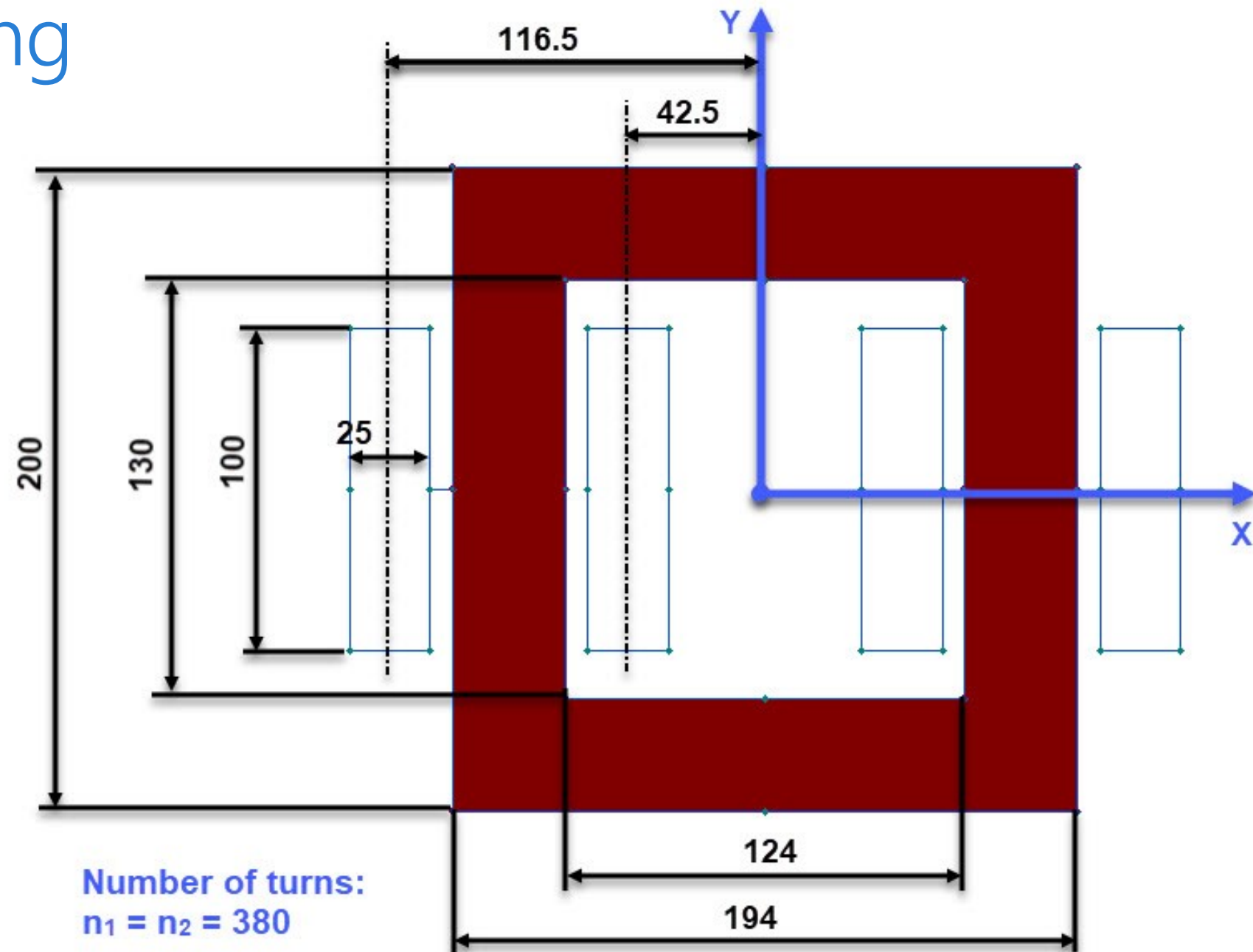


## 2. Schematic view

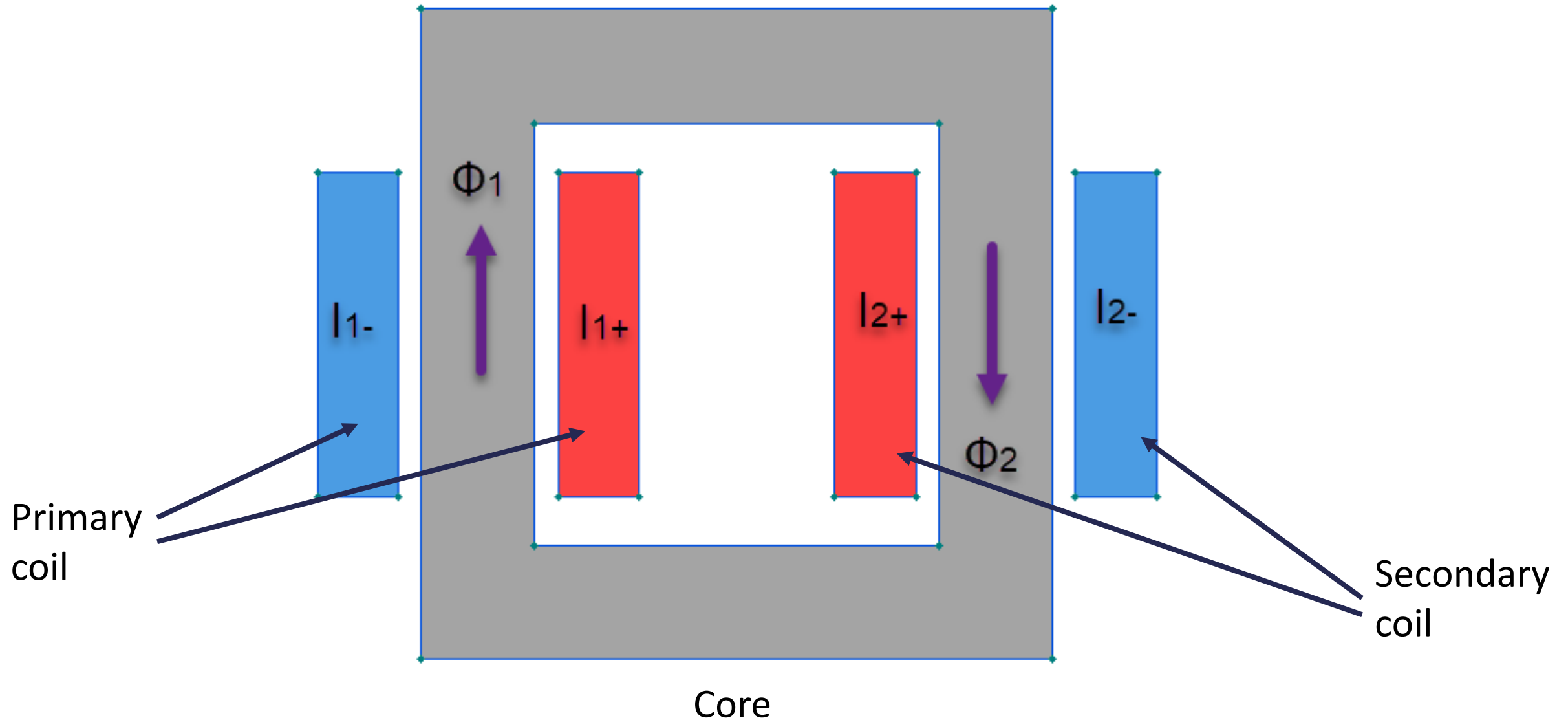


# Transformer sizing

Core depth  
(in Z-direction):  
 $L_z = 35 \text{ mm}$



# Transformer labels



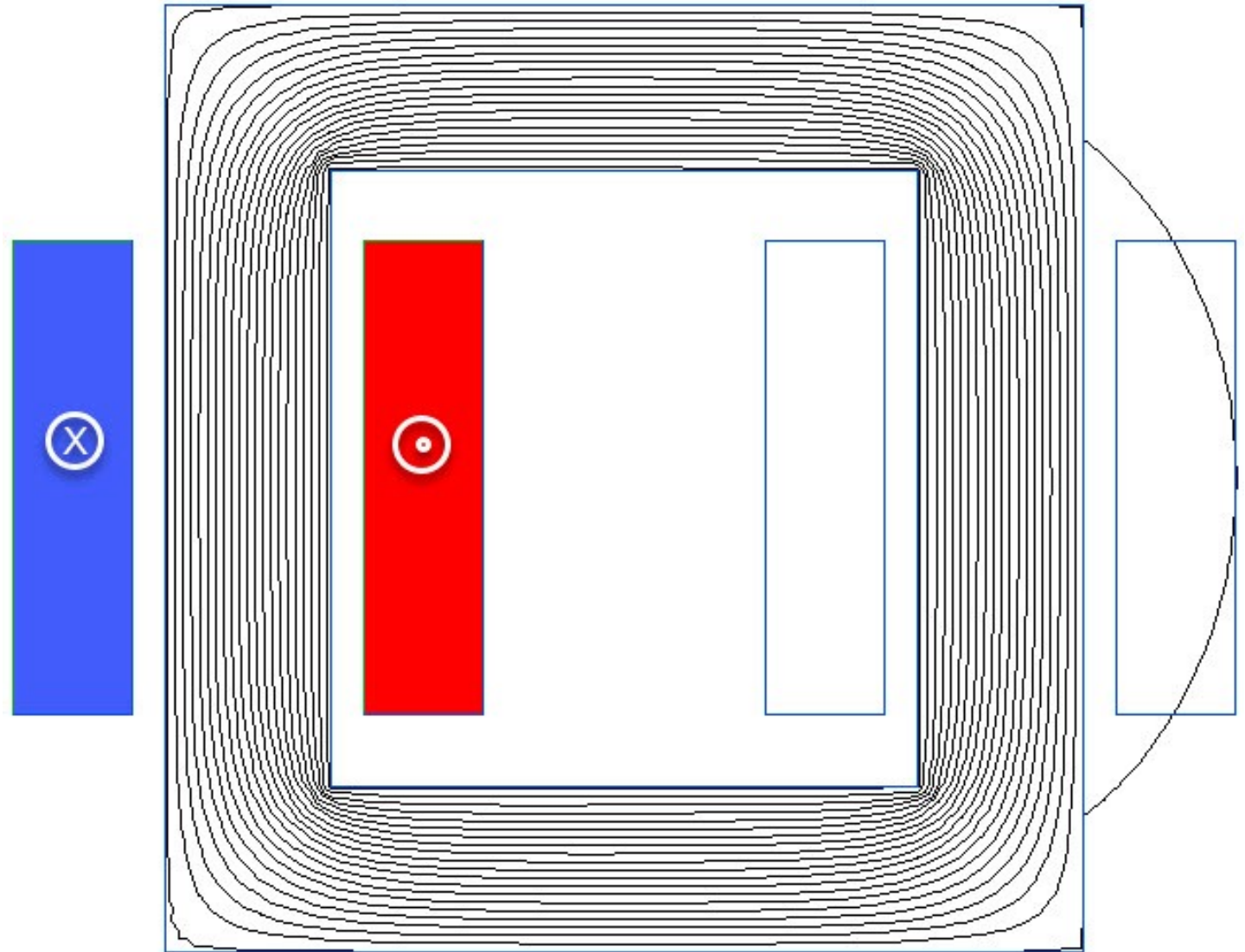
# No-load test:

Given:

The primary current  $I_1$

Calculate:

The secondary voltage  $V_2$



# Calculating induced voltage:

## 1. By flux linkage:

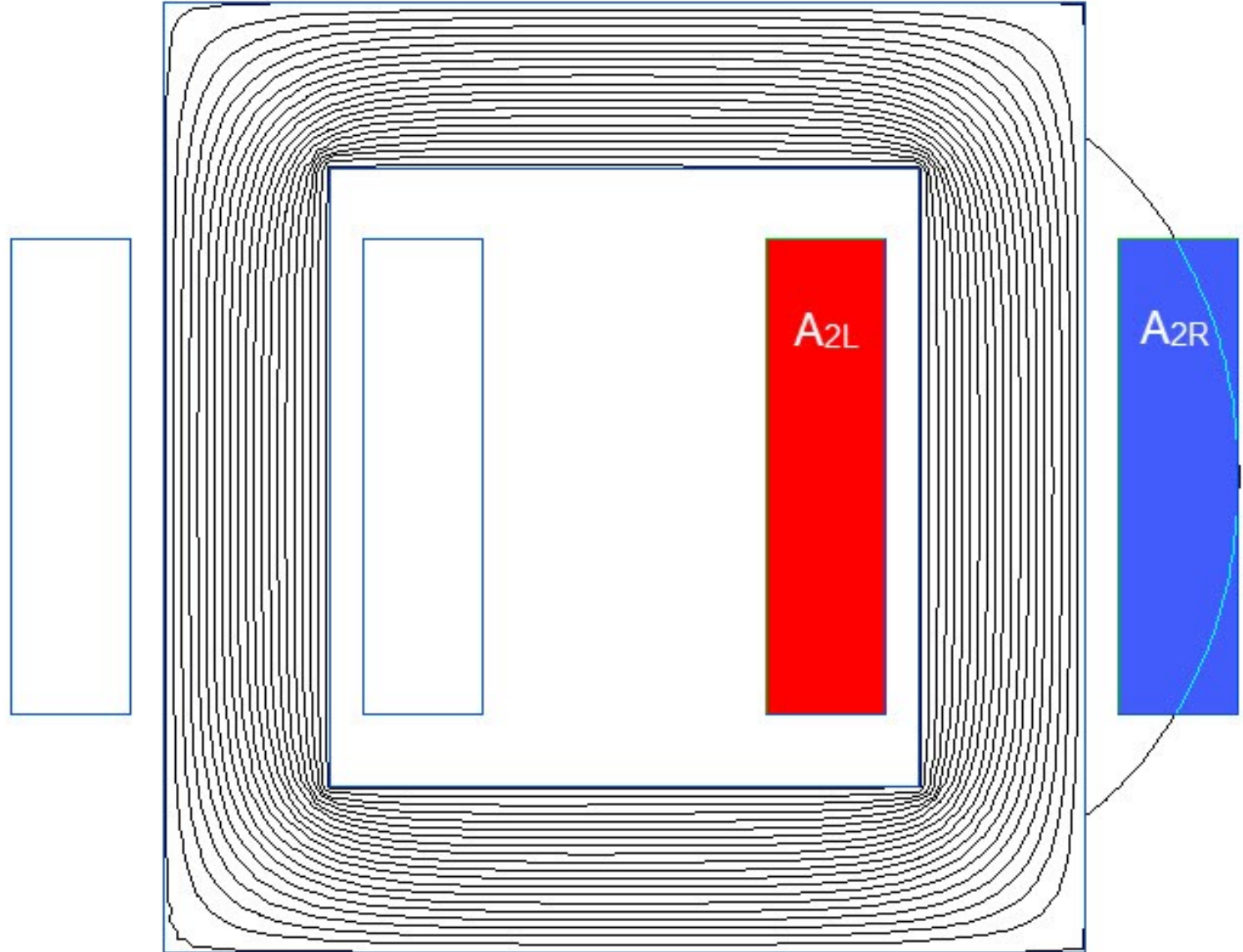
$$E = \frac{\partial \Psi}{\partial t} = \omega \Psi = \omega n(\Phi_L - \Phi_R)$$

## 2. By inductance:

$$E_1 = I_1 \cdot X_1 = I_1 \omega L_1$$

We can calculate inductance either

- by flux linkage  $L = \Psi/I$ , or
- by stored energy  $L = 2W/I^2$



# Calculating induced voltage:

## 1. By flux linkage:

$$E = \frac{\partial \Psi}{\partial t} = \omega \Psi = \omega n(\Phi_L - \Phi_R)$$

| Flux Linkage |             | secondary    | primary     |              |
|--------------|-------------|--------------|-------------|--------------|
| left         | $\Phi_{2L}$ | -7.13E-05 Wb | $\Phi_{1L}$ | 8.61E-07 Wb  |
| right        | $\Phi_{2R}$ | -3.73E-07 Wb | $\Phi_{1R}$ | -7.19E-05 Wb |
|              | $E_2$       | -8.47V       | $E_1$       | 8.69V        |

## 2. By inductance:

$$E_1 = I_1 \cdot X_1 = I_1 \omega L_1$$

We can calculate inductance either:

- by flux linkage  $L = \Psi/I$ , or
- by stored energy  $L = 2W/I^2$

| From Flux Linkage |        |          |      |
|-------------------|--------|----------|------|
| Flux Linkage:     | $\Psi$ | 0.03     | (Wb) |
| Current:          | $I$    | 0.12     | (A)  |
| Inductance:       | $L$    | 0.23049  | (H)  |
| From Energy       |        |          |      |
| Stored Energy     | $W$    | 1.66E-03 | J    |
| Current:          | $I$    | 0.12     | (A)  |
| Inductance:       | $L$    | 0.23035  | (H)  |
| <b>Voltage:</b>   | $E_1$  | 8.68     | V    |

# Calculate the short-circuit impedance:



## **Short-circuit impedance of a pair of windings:**

the voltage required to be applied at rated frequency to the terminals of a winding of a single-phase transformer, to cause the rated current to flow through these terminals when the terminals of the other winding are short-circuited.

The impedance voltage at rated current is usually expressed as a percentage of the rated voltage

# Opposite connection:

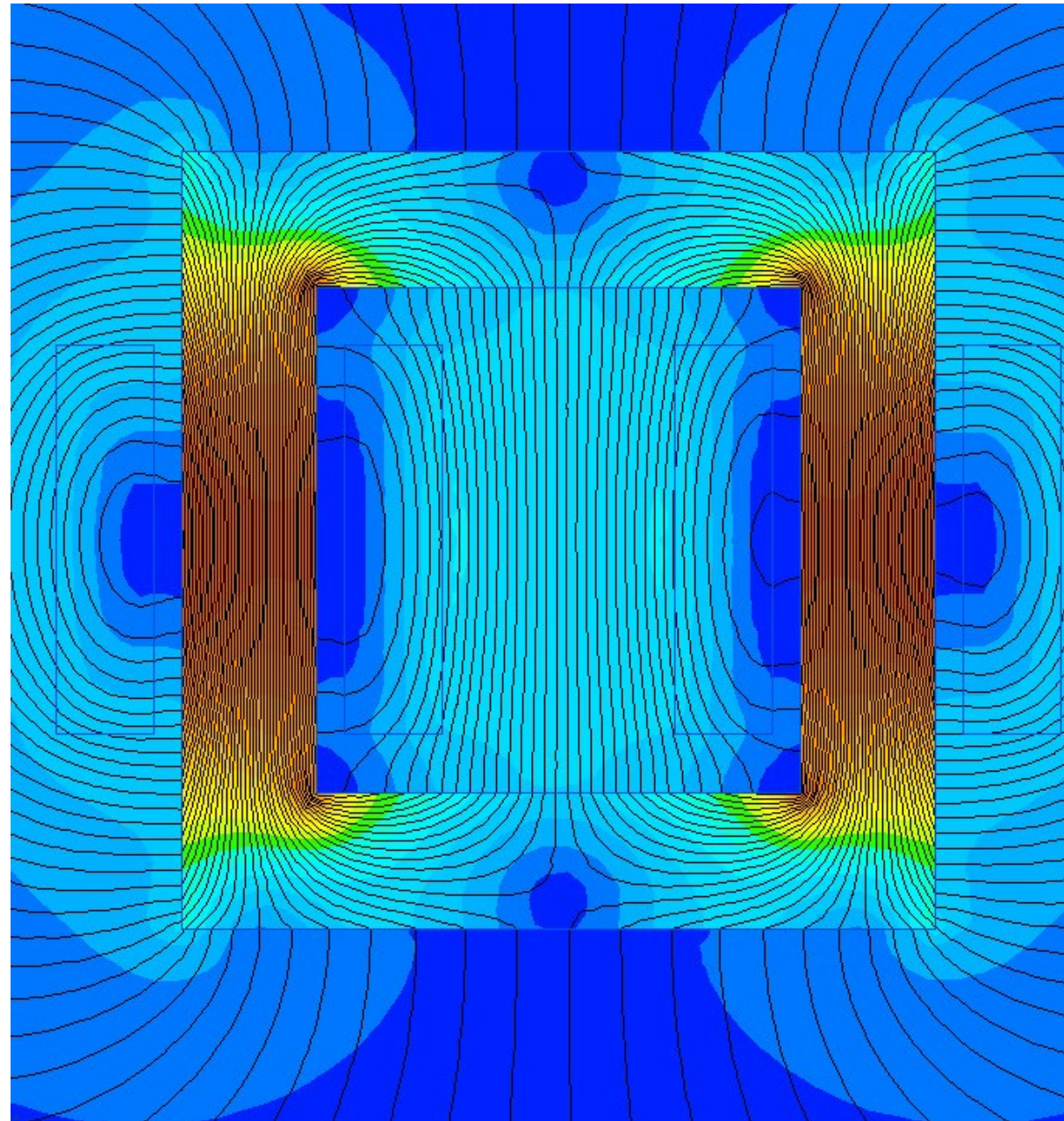
$$I_1 = -I_2$$

## By Energy:

|                       |               |   |
|-----------------------|---------------|---|
| $W$                   | 0.579269      | J |
| $I_1$                 | 10            | A |
| $L_\sigma = 2W / I^2$ | <b>0.0116</b> | H |

## By flux linkages:

|                               |                        |    |
|-------------------------------|------------------------|----|
| $\Phi_{prim+} - \Phi_{prim-}$ | $1.539 \cdot 10^{-4}$  | Wb |
| $\Phi_{sec+} - \Phi_{sec-}$   | $-1.539 \cdot 10^{-4}$ | Wb |
| $\Phi$                        | $3.078 \cdot 10^{-4}$  | Wb |
| $\Psi = n\Phi$                | $1.17 \cdot 10^{-1}$   | Wb |
| $L = \Psi / I$                | <b>0.0117</b>          | H  |



# Flux linkage with coils

$$I_1 = -I_2$$

**By Energy:**

|                       |               |   |
|-----------------------|---------------|---|
| $W$                   | 0.579269      | J |
| $I_1$                 | 10            | A |
| $L_\sigma = 2W / I^2$ | <b>0.0116</b> | H |

**By flux linkages:**

|                               |                        |    |
|-------------------------------|------------------------|----|
| $\Phi_{prim+} - \Phi_{prim-}$ | $1.539 \cdot 10^{-4}$  | Wb |
| $\Phi_{sec+} - \Phi_{sec-}$   | $-1.539 \cdot 10^{-4}$ | Wb |
| $\Phi$                        | $3.078 \cdot 10^{-4}$  | Wb |
| $\Psi = n\Phi$                | $1.17 \cdot 10^{-1}$   | Wb |
| $L = \Psi / I$                | <b>0.0117</b>          | H  |

